

**Solve each equation.**

1)  $2^{-r+2} = 2^{3r}$

2)  $3^{2m-1} \cdot 3^{-2m} = 3^{-3m}$

3)  $3^{-2x-1} = 243$

4)  $2^{-2x} = 4$

5)  $\log 3x^2 - \log 9 = 3$

6)  $\ln 8 + \ln (x+6) = 1$

7)  $\ln 4x + \ln 2 = 4$

8)  $\ln 9 + \ln 2x^2 - \ln 72$

9)  $\log (x-4) + \log 2 = \log 70$

10)  $\log 8 + \log 5x = \log 26$

11)  $\ln (x-5) + \ln 6 = 1$

12)  $\ln (x^2 + 7) + \ln 4 = 4$

**Solve each equation by factoring.**

13)  $k^2 = -63 - 16k$

14)  $n^2 = -48 - 15n$

15)  $8x^2 = 48x$

16)  $p^2 = 24 - 11p$

17)  $n^2 + 121 = -22n$

18)  $m^2 = -17m - 70$

19)  $7x^2 + 56 = -57x$

20)  $7r^2 - 57r = -8$

**Expand each logarithm.**

21)  $\log_6 (x \cdot y \cdot z^2)$

22)  $\log_5 (a^5 b^4)$

23)  $\log (a \cdot b \cdot c^6)$

24)  $\log_4 \left( \frac{12^6}{11} \right)^3$

**Condense each expression to a single logarithm.**

25)  $20\log_2 x - 5\log_2 y$

26)  $3\log_3 11 + 2\log_3 8$

**Rewrite each equation in exponential form.**

27)  $\log_a 29 = b$

28)  $\log_v 10 = u$

29)  $\log_m n = -15$

30)  $\log_x 87 = y$

**Solve each equation. Remember to check for extraneous solutions.**

31)  $1 + \frac{1}{r} = \frac{4}{r}$

32)  $\frac{1}{4m} + \frac{1}{4m^2} = \frac{1}{m^2}$

33)  $\frac{3}{4x^2} = \frac{1}{4x} + \frac{1}{4x^2}$

34)  $\frac{1}{6n^2} - \frac{1}{6n} = \frac{1}{n^2}$

35) Solve for  $x$ :  $\frac{12.3 - x}{4.5} = -0.83$

36) Solve for  $r$ :  $\sqrt{45 - r} = 5$

37) Solve for  $n$ :  $1.96\sqrt{\frac{0.5 \cdot 0.5}{n}} < 0.03$

38) If  $y = 10.2x^{0.72}$ , find  $y$  when  $x = 32.7$ .

39) Sketch the graphs of  $y = 2^x$  and  $y = 3^x$  on the same set of axes. Mark and label at least three points on each of the graphs. What point(s), if any, do they have in common? Write a description comparing the two graphs.

40) Sketch the graphs of  $y = \log_2 x$  and  $y = \log_3 x$  on the same set of axes. Mark and label at least three points on each of the graphs. What point(s), if any, do they have in common?

41) Write a description comparing the graphs of  $y = \log_2 x$  and  $y = 2^x$ .

**Solve each equation.**

1)  $2^{-x+2} = 2^{3x} \left\{ \frac{1}{2} \right\}$

2)  $3^{2m-1} \cdot 3^{-2m} = 3^{-3m} \left\{ \frac{1}{3} \right\}$

3)  $3^{-2x-1} = 243$   
 $\{-3\}$

4)  $2^{-2x} = 4$   
 $\{-1\}$

5)  $\log 3x^2 - \log 9 = 3$   
 $\{10\sqrt{30}, -10\sqrt{30}\}$

6)  $\ln 8 + \ln(x+6) = 1 \left\{ \frac{e-48}{8} \right\}$

7)  $\ln 4x + \ln 2 - 4 \left\{ \frac{e^4}{8} \right\}$

8)  $\ln 9 + \ln 2x^2 - \ln 72$   
 $\{2, -2\}$

9)  $\log(x-4) + \log 2 = \log 70$   
 $\{39\}$

10)  $\log 8 + \log 5x = \log 26 \left\{ \frac{13}{20} \right\}$

11)  $\ln(x-5) + \ln 6 = 1 \left\{ \frac{e+30}{6} \right\}$

12)  $\ln(x^2+7) + \ln 4 = 4 \left\{ \frac{\sqrt{e^4-28}}{2}, -\frac{\sqrt{e^4-28}}{2} \right\}$

**Solve each equation by factoring.**

13)  $k^2 = -63 - 16k$   
 $\{-9, -7\}$

14)  $n^2 = -48 - 15n$   
 $\{-4, -12\}$

15)  $8x^2 = 48x$   
 $\{-6, 0\}$

16)  $p^2 = 24 - 11p$   
 $\{-8, -3\}$

17)  $n^2 + 121 = -22n$   
 $\{-11\}$

18)  $m^2 = -17m - 70$   
 $\{-10, -7\}$

19)  $7x^2 + 56 = -57x$   
 $\left\{ -\frac{8}{7}, -7 \right\}$

20)  $7r^2 - 57r = -8$   
 $\left\{ \frac{1}{7}, 8 \right\}$

**Expand each logarithm.**

21)  $\log_6(x \cdot y \cdot z^2)$   
 $\log_6 x + \log_6 y + 2\log_6 z$

22)  $\log_5(a^5 b^4)$   
 $5\log_5 a + 4\log_5 b$

23)  $\log(a \cdot b \cdot c^6)$   
 $\log a + \log b + 6\log c$

24)  $\log_4 \left( \frac{12^6}{11} \right)^3$   
 $18\log_4 12 - 3\log_4 11$

Condense each expression to a single logarithm.

25)  $20\log_2 x - 5\log_2 y$

$$\log_2 \frac{x^{20}}{y^5}$$

26)  $3\log_3 11 + 2\log_3 8$

$$\log_3 (8^2 \cdot 11^3)$$

Rewrite each equation in exponential form.

27)  $\log_a 29 = b$

$$a^b = 29$$

28)  $\log_v 10 = u$

$$v^u = 10$$

29)  $\log_m n = -15$

$$m^{-15} = n$$

30)  $\log_x 87 = y$

$$x^y = 87$$

Solve each equation. Remember to check for extraneous solutions.

31)  $1 + \frac{1}{r} = \frac{4}{r}$

$$\{3\}$$

32)  $\frac{1}{4m} + \frac{1}{4m^2} = \frac{1}{m^2}$

$$\{3\}$$

33)  $\frac{3}{4x^2} = \frac{1}{4x} + \frac{1}{4x^2}$

$$\{2\}$$

34)  $\frac{1}{6n^2} - \frac{1}{6n} = \frac{1}{n^2}$

$$\{-5\}$$

35) Solve for  $x$ :  $\frac{12.3 - x}{4.5} = -0.83$

$$x = 16.035$$

36) Solve for  $r$ :  $\sqrt{45 - r} = 5$

$$r = 20$$

37) Solve for  $n$ :  $1.96\sqrt{\frac{0.5 \cdot 0.5}{n}} < 0.03$

$$n > 1067.11$$

38) If  $y = 10.2x^{0.72}$ , find  $y$  when  $x = 32.7$ .

$$y = 125.62$$

39) Sketch the graphs of  $y = 2^x$  and  $y = 3^x$  on the same set of axes. Mark and label at least three points on each of the graphs. What point(s), if any, do they have in common? Write a description comparing the two graphs.

40) Sketch the graphs of  $y = \log_2 x$  and  $y = \log_3 x$  on the same set of axes. Mark and label at least three points on each of the graphs. What point(s), if any, do they have in common?

41) Write a description comparing the graphs of  $y = \log_2 x$  and  $y = 2^x$ . Since the functions are inverses of each other, the graphs are reflections of each other across the line  $y = x$ .